

Consider your "Bounce that Ball" data:

$$x \frac{1}{2} \left(\begin{array}{l} 80 \text{ cm drop} \rightarrow 60 \text{ cm bounce} \\ 40 \text{ cm drop} \rightarrow 30 \text{ cm bounce} \end{array} \right) x \frac{1}{2}$$

Working with Proportionalities in Physics

If you have a linear graph with a y-intercept of zero (i.e. "Bounce that Ball"), then this suggests a direct proportionality.

"is proportional to" $y \propto x$ \propto
 "y is directly proportional to x"
 "y varies directly with x"

Consider your bounce that ball data:

$$h_b \propto h_d \quad (\text{proportionality statement})$$

$$h_b = k h_d \quad (\text{general equation})$$

↑ proportionality constant.

$$\frac{60 \text{ cm}}{80 \text{ cm}} = k \left(\frac{80 \text{ cm}}{80 \text{ cm}} \right)$$

$$k = 0.75 \quad (\text{proportionality constant})$$

$$h_b = 0.75 h_d \quad (\text{specific equation})$$

$$y = mx + b$$

A graph of h_b vs h_d will be linear with a slope of k and a y-intercept of zero.

Examples of a proportionality statement.

$A \propto B^2$ "A is proportional to the square of B"

"A is directly proportional to B^2 "

"A varies directly with the square of B"

$$F \propto \frac{v^2}{r}$$

"F varies directly with the square of v and inversely with r"